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Compositional data techniques for the analysis of the container traffic share in a multi-port region

M. Grifoll[*] ⓘ, M. I. Ortego and J. J. Egozcue

Abstract

The statistical techniques based on compositional data are applied to investigate the evolution of the traffic share of the container throughput in a multi-port system. Compositional vectors are those which contain relative information of parts of some whole. The application of conventional statistical techniques to compositional data may lead to erroneous conclusions and spurious correlations. Therefore, compositional data (CoDa) should be treated taking into account their own mathematical structure. The so-called log-ratio approach provides a set of transformations that allow to apply conventional statistical techniques to the transformed compositional data samples. Thus, the objective of this paper is double. As a first stage it aims to introduce the CoDa formalism and highlight its potentiality in the port container throughput analysis as example of transport system providing an applied example: the container throughput evolution in the Spanish Mediterranean Ports system during the period 1976–2015. Second, based on the previous analysis, the aim is to characterize the container throughput in SpanishMed ports and its temporal evolution. The CoDa analysis clarifies the interpretation and data association of the container traffic throughput evolution in function of some selected change points: boom of containerization in 1990s and 2008 crisis. This contribution proves that the CoDa methodology is useful to investigate the complexity of the transport disciplines in order to understand and to manage the spatial integration that results from the movement of people and freight.

Keywords: Multi-port system, Traffic share, Container throughput, Compositional data, SpanishMed

1 Introduction

Transport disciplines are motivated to explain the spatial integration that result from the movement of people and freight from one place to another. From a descriptive point of view, several contributions seek to understand the spatial organization of mobility considering its attributes and constraints (e.g. [6–9, 15, 17, 22, 25, 26, 30, 32]). Terminals, modes and networks are the basis of complex systems under constant evolution influenced by the geo-spatial economy development (with private and public agents), growth of infrastructures and physical restrictions. The development of methodological strategies has allowed to describe and explain transport systems

according to its evident complexity. This contribution pursues the introduction of Compositional Data (CoDa) methodology in the transport system analysis using as example the evolution of the container traffic in the Spanish Mediterranean Sea (SpanishMed) port system.

Containerization plays an important role in the maritime transport and in the global economy growth. Since the first wave of containerization (1970s), the global container traffic has been reformulated seeking economy of scales and more efficient distribution systems (e.g. hub-and-spoke model or transshipment activity). In this sense, the container throughput share of ports has evolved at the same time that the industrial regions and global trade have shifted. Also, shippers and logistic providers select a chain where the port is merely a node [25]. In the recent years, new container ports have emerged as relevant actors in container throughput at the same time that other ports have gradually lost their relevance. An S-shaped curve has been observed in the traffic evolution of world ports

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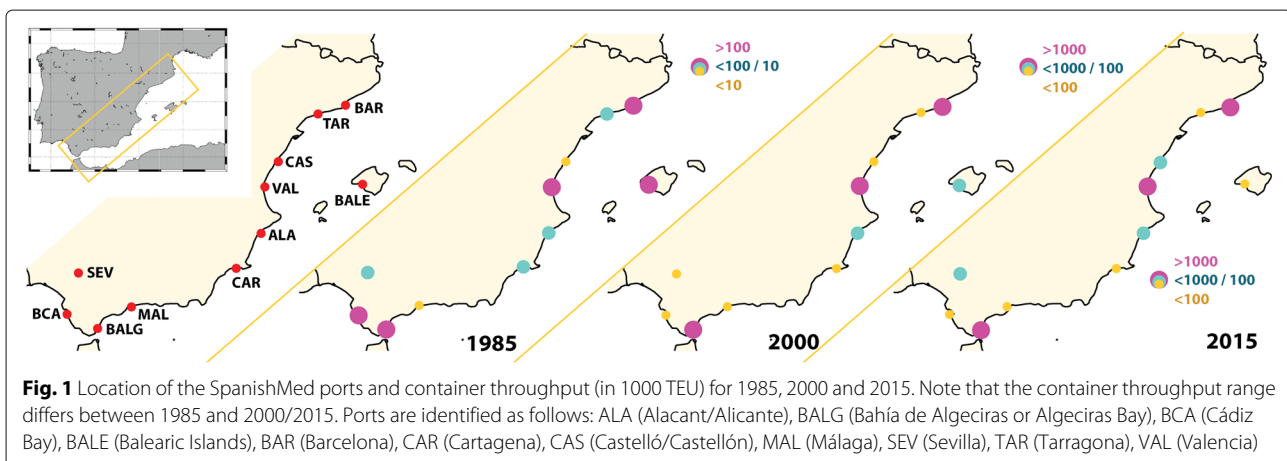
(increasing rapidly in the late 1970s and slowing down in 2000s, according to [18]) with a consequent shifting in the traffic share. In the European context, the traffic share analysis of recent years suggests a concentration process in a dozen large container ports [24, 25]. One motivation is the transshipment activity which leads to the emergence of hub ports capturing high capacity shipping lines and acting as pure transshipment nodes (e.g. Bahía de Algeciras or Goia Tauro ports). This tendency is accompanied by the increase of the competition among terminal operators and the establishment of shipping lines at ports acting as local hubs (for instance, the MSC choice of Valencia port as a local hub for its transshipment activity). The mentioned investigations on the port traffic market use simple statistical techniques based on traffic share as a percentage of a whole. This simple approach, which considers the container flow data pertaining to a real sample space, has lead to a considerable understanding of the port competition and traffic concentration. However, neglecting the compositional character of the traffic share data (i.e. as a parts of a whole) may lead to erroneous conclusions. Pearson [29] found that standard statistical techniques loose their applicability and classical interpretation when applied to compositional data. Spurious correlations may arise from the use of conventional statistical techniques with proportions. In this sense, establishing correlations, data associations and tendencies among the traffic share of ports should be addressed using Compositional Data Analysis (CoDa). CoDa techniques allow to reveal underlying patterns of the data structure providing a straightforward interpretation.

Since the seminal work of [1], Compositional Data analysis techniques have been used with successful results simultaneously that a consistent mathematical framework has been developed [28]. The established CoDa mathematical structure includes a definition of the appropriate sample space for this type of data. The properties of compositional data arise from the fact that they convey relative information. In fact, compositional data are equivalence classes of proportional vectors quantifying shares. However, it is usual to express them using a representative of the equivalence class, that is, applying the closure operation to them. CoDa vectors, turned into vectors of proportions, have relevant numerical properties with consequences to their statistical analyses. For instance, spurious correlations may arise when computing correlations between the parts of the composition using the full composition or only a sub-composition [3, 28, 29]. This is known as a sub-compositional incoherence. In consequence, the standard statistical techniques used for real, unconstrained variables should not be used for the analysis of compositional data. Further discussions of the compositional properties and their consequences in practical cases are found in [28] among others. CoDa techniques have been applied to problems in many areas of science such as social sciences [19], earth science [20], climate change [23], production engineering [31], geostatistics [12] or economy [16]. These works remark the suitability of the CoDa methodology for a proper interpretation of data sets when we focus on the relative information rather than the absolute amounts.

In this sense, the novel application of CoDa methods to the analysis of container flows in ports is an excellent opportunity to introduce this methodology in the field of transport analysis. We will follow the research sequence recommended for most practitioners of CoDa. This sequence is composed of three steps: 1st represent CoDa in log-ratio type coordinates, 2nd apply standard statistical analysis to the coordinates as real random variables and 3rd interpret results in coordinates and/or in terms of the original components [21, 28].

In our case, the compositional approach allows to study the evolution of the container throughput from a relative perspective. In this work, we have selected the Spanish ports located in the Mediterranean range (SpanishMed). This area includes 11 ports. The location of these ports is shown in Fig. 1. The SpanishMed area covers a relevant market in the European context and includes two

Fig. 1 Location of the SpanishMed ports and container throughput (in 1000 TEU) for 1985, 2000 and 2015. Note that the container throughput range differs between 1985 and 2000/2015. Ports are identified as follows: ALA (Alacant/Alicante), BALG (Bahía de Algeciras or Algeciras Bay), BCA (Cádiz Bay), BALE (Balearic Islands), BAR (Barcelona), CAR (Cartagena), CAS (Castelló/Castellón), MAL (Málaga), SEV (Sevilla), TAR (Tarragona), VAL (Valencia)

of the top ten European ports in container throughput: Valencia and Bahía de Algeciras. The hinterland of this region extends to a high portion of Spain and South of France, competing with Portuguese and North African ports to capture container transshipment activity.

The objective of this paper is double. As a first stage it aims to introduce the CoDa formalism and highlight its potentiality in the port container throughput analysis as example of transport system providing an applied example: SpanishMed ports. Second, based on the previous analysis, the aim is to characterize the container throughput in SpanishMed ports and its temporal evolution.

The contribution is organized as follows: a short description of the container throughput evolution of the SpanishMed ports is presented (Section 2). Then, the CoDa methodology is briefly introduced (Section 3). The results from the CoDa exploratory tools are shown in Sections 4 and 5 for a sub-sample and for the whole system respectively. In Section 6 results are discussed, remarking the insight provided by CoDa techniques in the SpanishMed ports analysis as example of research in transport discipline.

2 SpanishMed port system

The state-owned Spanish Port System includes 46 ports of general interest, managed by 28 Port Authorities, whose coordination and efficiency control corresponds to the Spanish Port Agency (Puertos del Estado; www.puertos.es), a body seconded by the Ministry of Public Works that is responsib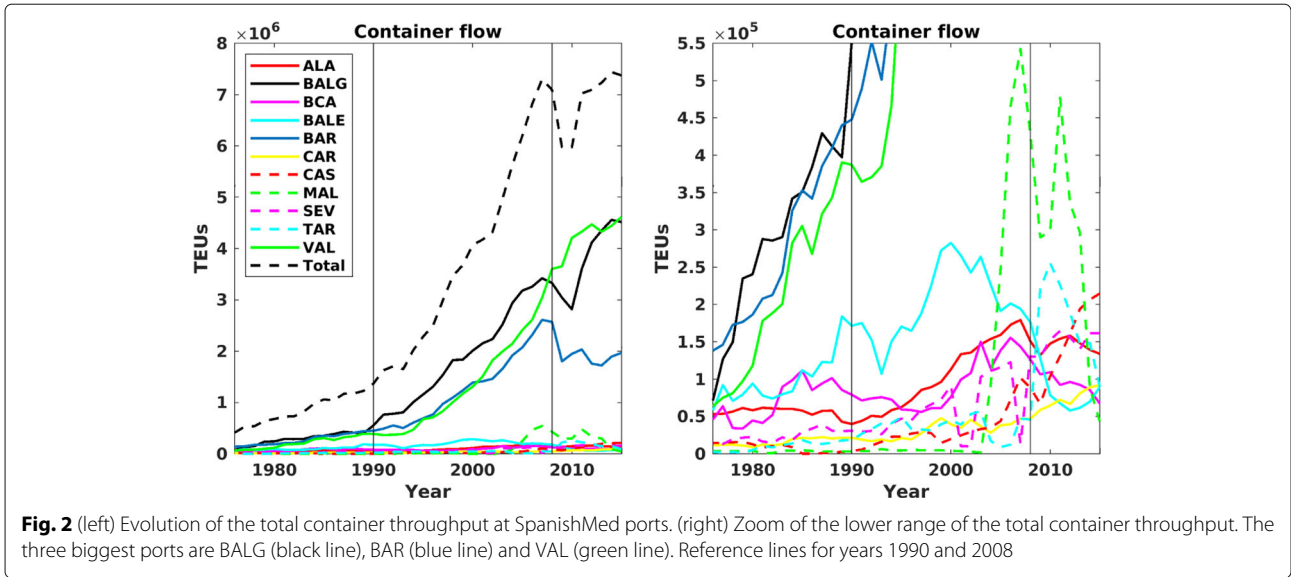le for implementing the government's port policy. SpanishMed ports include 11 Port Authorities (see Fig. 1). The data were obtained from the Spanish Port Agency (integrated annual data). Small ports, some of them owned by regional governments, are excluded from this analysis because their container throughput is negligible. The total container throughput in SpanishMed arose 11.988.405 TEU (Twenty-foot Equivalent Unit) during 2015. The main ports are Algeciras Bay, Valencia and Barcelona covering a traffic share of 37.67%, 16.39% and 38.50% respectively during 2015 (see Table 1). A preliminary analysis indicates that port throughput concentration occurs according to the traffic evolution for the period 1976–2015 according to the normalized Herfindahl-Hirschman index [24] shown in Table 1. More than 90% of the traffic during 2015 corresponds to these three ports, with also large percentages for 2000, 1985 and 1976 (87.5%, 73.9% and 57.5% respectively).

The temporal evolution of the Spanish Med container throughput is shown in Fig. 2 in terms of total traffic evolution. The container flow at SpanishMed has a containerization peak growth (1995–2010) followed by a maturity phase (2010-today). This suits well in a K-wave behavior which specific phases in container port development are taking place, such as introduction, acceleration, peak growth and maturity [18]. Considering only the "three-big" ports, the evolution of the traffic share at the SpanishMed system shows a gentle decreasing of the Barcelona and Algeciras Bay port traffic as opposite to an increase of Valencia Port after 2007 (crisis period). Among other motivations this behaviour is due to the 2002 selection of

Table 1 Total number of containers (in TEU) and traffic share (in %) for the SpanishMed ports during years 1976, 1985, 2000 and 2015

Port	1976		1985		2000		2015	
	Container through.	Traffic	Container through.	Traffic	Container through.	Traffic	Container through.	Traffic
ALA	53009	11.15	57783	4.24	113110	2.10	133880	1.12
BALG	71313	15.01	350573	25.70	2009122	37.37	4515768	37.67
BCA	45926	9.67	111522	8.18	76361	1.42	67312	0.57
BALE	57967	12.20	111909	8.20	282451	5.25	89474	0.75
BAR	138182	29.08	352799	25.86	1387570	25.81	1965262	16.39
CAR	11500	2.42	21333	1.56	39501	0.73	92036	0.77
CAS	14654	3.08	309	0.02	19783	0.37	214663	1.79
MAL	3606	0.76	4764	0.35	4062	0.08	43282	0.36
SEV	12781	2.69	29617	2.17	91095	1.69	161671	1.35
TAR	2576	0.54	18327	1.34	44855	0.83	89862	0.75
VAL	63593	13.38	305230	22.37	1308010	24.33	4615196	38.50
H*		0.080		0.119		0.196		0.250
$\|\mathbf{x}\|_a^2$		4.096		6.716		6.128		5.441

Ports are identified as follows: ALA (Alacant/Alicante), BALG (Bahía de Algeciras or Algeciras Bay), BCA (Cádiz Bay), BALE (Balearic Islands), BAR (Barcelona), CAR (Cartagena), CAS (Castelló/Castellón), MAL (Málaga), SEV (Sevilla), TAR (Tarragona), VAL (Valencia). The values of the normalized Herfindahl-Hirschman index (H*) and squared Aitchison norm $\left(\|\mathbf{x}\|_a^2\right)$ are also shown

Fig. 2 (left) Evolution of the total container throughput at SpanishMed ports. (right) Zoom of the lower range of the total container throughput. The three biggest ports are BALG (black line), BAR (blue line) and VAL (green line). Reference lines for years 1990 and 2008

Valencia as the hub port for MSC shipping company and the good response of the transshipment flow in Valencia after the crisis. The Barcelona container traffic was hit hard by the crisis with a significant decrease of container flow (from 2.6 million TEUs during 2008 to 1.8 million TEUs in 2009). Actually an equal percentage of traffic share occurs between Valencia and Algeciras Bay (both of them with relevant percentage of transshipment flows) followed from a certain distance by the Barcelona port, which its traffic is mainly focused on the import/export activity.

3 The CoDa methodology

Compositional Data (CoDa) are defined as a quantitative description of the parts of a whole [28]. In fact, a composition is a class of equivalence, i.e., proportional vectors provide the same compositional information. Usually, a representative of the class of equivalence is chosen. The suitable sample space for the representation of compositional vectors is the Simplex (S^D) (Eq. 1):

$$S^D = \left\{ \mathbf{x} = [x_1, x_2, ...x_n] : x_1 > 0, x_2 > 0, \ldots, x_n > 0; \sum_{i=1}^{D} x_i = c \right\}. \quad (1)$$

A composition $\mathbf{x} = [x_1, \ldots, x_D]$ is defined as a vector with D strictly positive components adding to a constant (c), where the constant c is the closure. The closure is the vector operation assigning the constant sum representative of the composition. Frequently, c is 100 for measurements represented in percentages. The simplex is characterized as a vector space using two operations: perturbation and powering [28]. The so-called Aitchison geometry for the simplex also includes a distance. The Aitchison

distance between two compositions $\mathbf{x} = [x_1, \ldots, x_D]$, $\mathbf{y} = [y_1, \ldots, y_D]$ is defined as (Eq. 2):

$$d_a(\mathbf{x}, \mathbf{y}) = \sqrt{\frac{1}{2D} \sum_{i=1}^{D} \sum_{j=1}^{D} \left(\ln \left(\frac{x_i}{x_j} \right) - \ln \left(\frac{y_i}{y_j} \right) \right)^2}, \quad (2)$$

and the corresponding norm is (Eq. 3):

$$\|\mathbf{x}\|_a = \sqrt{\frac{1}{2D} \sum_{i=1}^{D} \sum_{j=1}^{D} \left(\ln \frac{x_i}{x_j} \right)^2}. \quad (3)$$

The principles of compositional analysis include three conditions that should be fulfilled by the statistical methods that are applied to compositions: scale invariance, permutation invariance, and subcompositional coherence [2, 28]. In subsequent sections we will take advantage of the subcompositional coherence property for the treatment of the container throughput in the SpanishMed port system.

Given a sample of size n of D-part compositional vectors, $\mathbf{X}$, $[x_{11}, \ldots, x_{1D}], \ldots [x_{n1}, \ldots, x_{nD}]$, it is usual to describe them using central tendency and variability measures. The standard statistical descriptive measures, based on the real Euclidean structure, applied to Compositional Data may lead to erroneous conclusions. An alternative set of descriptive measures, based in the Aitchison geometry has been defined. The center (cen), Eq. 4, is a measure of central tendency of the compositional sample:

$$\text{cen}(\mathbf{X}) = [g_1, \ldots, g_D], \quad (4)$$

being g_i the column-wise geometric mean:

$$g_j(x) = \left(\prod_{i=1}^{n} x_{ij} \right)^{1/n}, j = 1, 2, \ldots, D. \quad (5)$$

The definition of the concept of distance between two compositions (Eq. 2) is relevant for the statistical analysis of compositional data because it allows to define basic statistical concepts such as variability. The variation matrix is a measure of the data dispersion and it is defined in terms of pairwise log-ratio variances (Eq. 6) [2, 28]:

$$\mathbf{T} = \begin{pmatrix} 0 & t_{12} & \ldots & t_{1D} \\ t_{21} & 0 & \ldots & t_{2D} \\ \vdots & \vdots & \ddots & \vdots \\ t_{D1} & t_{D2} & \ldots & 0 \end{pmatrix}, \, t_{ij} = \text{var}\left(\ln\frac{x_i}{x_j}\right). \quad (6)$$

The sample total variance (Eq. 7) is a measure of global dispersion of the compositional sample, being a summary of the variation matrix in a single quantity.

$$\text{totvar}(\mathbf{X}) = \frac{1}{2D} \sum_{i,j=1}^{D} \text{var}\left(\ln\frac{x_i}{x_j}\right) = \frac{1}{2D} \sum_{i,j=1}^{D} t_{ij}. \quad (7)$$

Also, Aitchison norm (Eq. 3) may provide an estimation of the concentration level of container throughput ports similar to Herfindahl-Hirschman index.

The mathematical structure of the Simplex as an Euclidean vector space gives the possibility of treating compositional data in a suitable manner. However, the fact that the information given by compositions is relative was the origin of the so-called principle of working in coordinates [2, 21]. That is, transforming compositions into real vectors, for which the usual real Euclidean structure is suitable. Several transformations based on log-ratios have been defined in the literature [2, 13]. Historically, the additive log-ratio (*alr*) was the first to be used and the centered-log ratio (*clr*) appeared later; both introduced by [1, 2]. The third family of transformations is the *ilr* (isometric log-ratio transformation) which provides Cartesian orthonormal coordinates [13]. The clr transformation of a composition $\mathbf{x} = [x_1, \ldots, x_D]$ is:

$$clr(\mathbf{x}) = \ln\left(\frac{x_1}{g_m(\mathbf{x})}, \frac{x_2}{g_m(\mathbf{x})}, \frac{x_3}{g_m(\mathbf{x})}, \ldots, \frac{x_D}{g_m(\mathbf{x})}\right), \quad (8)$$

where $g_m(\mathbf{x})$ denotes the geometric mean of the parts (Eq. 9).

$$g_i(x) = \left(\prod_{i=1}^{D} x_i\right)^{1/D}. \quad (9)$$

The mentioned transformations (alr/clr/ilr) have different properties. The alr transformation has the inconvenience that the transformation is not isometric, i.e. it does not preserve distances. This implies that the use of the inner-product or the determination of the angle between two vectors became more difficult [11]. The clr-transformation keeps the same number of components

as the number of parts in the composition: a composition with D parts is transformed into D real components adding up to 0 [13]. This transformation preserves the metrics (i.e. the distances and the angles). That is, the distance between two compositions measured in the Simplex using the Aitchison distance (Eq. 2) and the distance between their transformed vectors using the usual real Euclidian distance are the same. Therefore, the clr-transformation may be useful as exploratory tools based on metrics, such as the clr-biplot. However, the clr-transformation has the inconvenience that the covariance and correlation matrix are singular (i.e their determinant is zero), due to the zero-sum of the transformed vectors.

The isometric log-ratio transformation (ilr) [13] appears as an alternative when statistical tools based on covariances are needed. Compositions are expressed as coordinates with respect to an orthonormal basis. This transformation corresponds to an isometry of vector spaces between the simplex of D-parts (S^D) (Eq. 1) and $\mathbb{R}^{D-1}$. In order to enhance interpretability, an orthonormal basis linked to a Sequential Binary Partition (SBP) is often selected [28]. The SBP is encoded through a sign matrix, that allows the practitioner to define a hierarchy of the parts of the composition based on knowledge about the problem at hand. The coordinates obtained in such manner are called balances, and they are the normalized log-ratios of the geometric mean of the groups of parts defined by the sign matrix at each step. Balances have the form (Eq. 10):

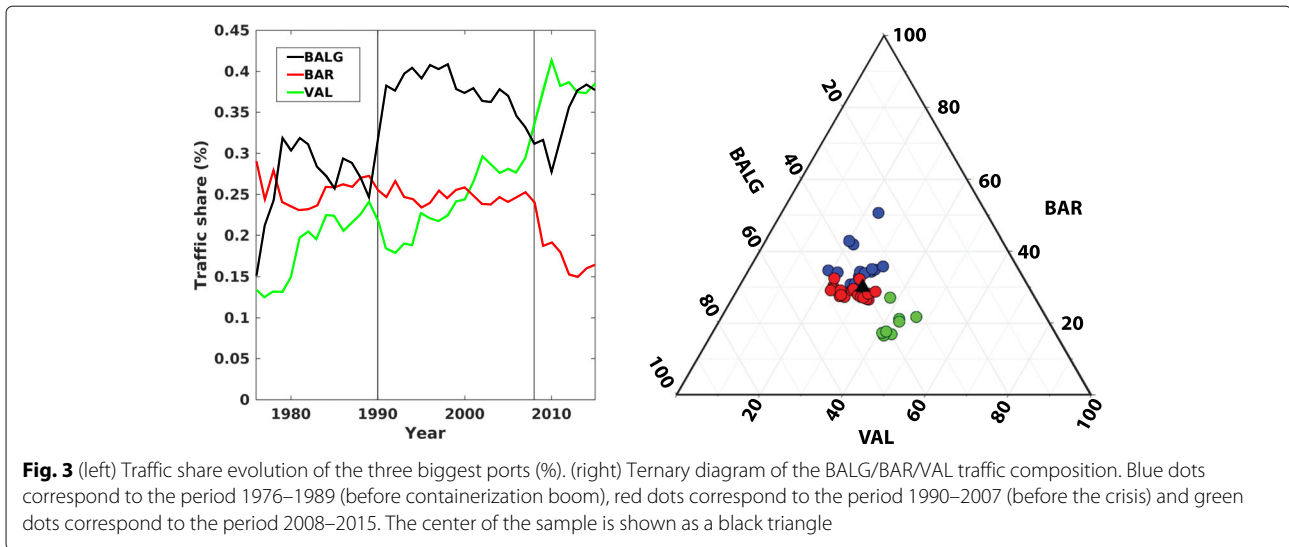$$b_j = \sqrt{\frac{rs}{r+s}} \ln\frac{g_m(x+)}{g_m(x-)}. \quad (10)$$

where r and s are the number of parts in the $+1$-group and -1-group respectively.

4   Subcompositional analysis of SpanishMed: BALG, BAR and VAL.

In order to introduce the compositional methodology in the SpanishMed system, this section focuses only in the subcomposition formed by the three biggest ports: Algeciras Bay (BALG), Barcelona (BAR) and Valencia (VAL; see all acronyms in Fig. 1). The subcompositional coherence property ensured by the compositional approach guarantees that the results obtained for this subsample will be coherent with the results obtained for the whole system. As we mention previously, these three ports have reached 90% of the traffic share in SpanishMed in the recent years (see Fig. 2 and Table 1). Figure 2 shows the raw traffic evolution for the SpanishMed system where these three ports show a relevant role in the traffic share. There is an increasing trend in traffic, although there are some ups and downs since 2008.

Figure 3 shows the traffic share evolution for the three biggest ports considered as a port system. The relative

Fig. 3 (left) Traffic share evolution of the three biggest ports (%). (right) Ternary diagram of the BALG/BAR/VAL traffic composition. Blue dots correspond to the period 1976–1989 (before containerization boom), red dots correspond to the period 1990–2007 (before the crisis) and green dots correspond to the period 2008–2015. The center of the sample is shown as a black triangle

contribution of each port has a different interpretation in comparison to the total traffic (Fig. 2). It means, two of the ports increase their share (BALG and VAL), whilst the third one (BAR) loses relative importance. From a temporal point of view, this may be linked to three main events: the boom of the containerization in the 1990s, the selection of VAL Port as a basis for shipping company MSC in 2002 (and its posterior development as a transshipment hub) and the 2008 crisis. The crisis effects implied a decrease of the total container throughput (see Fig. 2). These change points in the traffic evolution are also observed if the traffic share is represented using a ternary plot (Fig. 3). The ternary plot is a barycentric plot which graphically depicts the ratios of the three variables as positions in an equilateral triangle. The figure shows the temporal evolution of the compositions of the traffic share considering the containerization boom in 1990 and the post-crisis (see blue, red and green colored points). The evolution of the cloud of points shows a predominance of BAR during the initial years (before containerization; blue points), the prevalence of BALG port after the containerization (red points) and the leadership in traffic share of VAL port after the crisis/MSC settling effect (green points).

The center of this cloud of points (i.e. the center of the sample of compositions, Eq. 4, marked with a black triangle) is near to the baricenter of the triangle, with a slight shift due to the influence of BALG port. The sample center value is shown in Table 2. From a historical point of view the center reveals a predominance of the BALG port with a more than 40.2% of the traffic share. Table 2 also shows the variability of the composition (variation array in Eq. 6). The maximum variability is associated to BAR port (e.g. variances equal to 0.146 and 0.216) due to the traffic fluctuations caused by the 2008 crisis.

The principal components for compositional data were introduced by [5]. The biplots for compositional data (clr-biplots) were introduced by [4] and they have been a powerful tool for multivariate analysis [10, 28]. The clr-biplot is an exploratory tool that allows to display data and variables in the same plot. The dimensionality of the dataset is reduced, as the original information is represented in a projection on two new variables. A principal component analysis of the clr-transformed compositions is performed. The clr-biplot corresponds to the projection of the information of the dataset in the 2-dimensional plane formed by the two first components. The visual interpretation of clr-biplots differs slightly from that of the general biplots. Form and covariance clr-biplots highlight different characteristics of the data in the projection. The form clr-biplot helps with the assessment of the goodness of the representation of the variables in the projection. The covariance clr-biplot helps with the assessment of the variability and relationships between the variables. The principal elements of interpretation of clr-biplots are the rays and the links formed by the rays. Some rules were highlighted by [10]. For instance, if three rays are aligned, then the relation between these parts is linear up to the quality of the projection. Also, orthogonal links mean that two sub-compositions are uncorrelated. The covariance
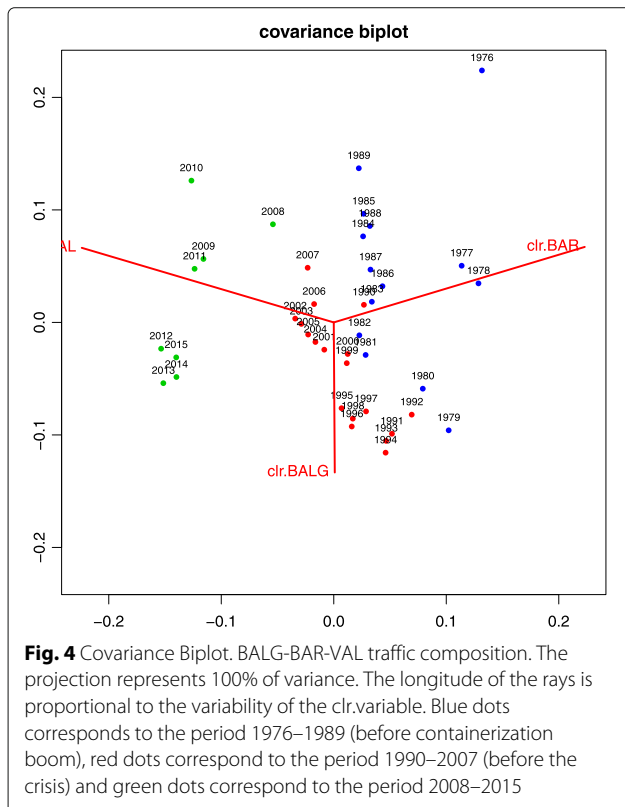
Table 2 Variation array of the traffic throughput yearly composition

Port	BALG	BAR	VAL	cen(x) (%)
BALG	0.000	0.146	0.103	40.2
BAR	0.146	0.000	0.216	30.0
VAL	0.103	0.216	0.000	29.8

The centre for each port is also shown in an additional column

clr-biplot includes specific information of the variability through the length of the rays.

The covariance clr-biplot of the three big ports (BALG-BAR-VAL) is presented in Fig. 4. The shown projection represents 100% of the variance and the three variables are exactly represented in the form clr-biplot, so it is omitted for simplicity. The longitude of the rays in the covariance biplot (Fig. 4) is proportional to the variability of the clr-variable. BALG is slightly less variable than VAL and BAR ports. This reflects the aforementioned traffic variation array of Table 2, where the maximum pairwise variance is between BAR and VAL. The position of the yearly compositions in the graph suggests a temporal evolution. In the initial years, the points are near to BAR ray, then shifting towards BALG ray in the first waves of containerization (red points). Since the 2000's there is an evolution towards VAL ray (green points). This increase is more moderate since the start of the crisis; but the influence of the pair VAL – BALG is reinforced in contrast to BAR. Figure 2 highlights the change points defined before: the boom of the containerization that attracted traffic to BALG and the combined effect of the MSC settling in VAL and the crisis attracting traffic to VAL. After the crisis the evolution is clear: VAL maintains its influence, but BALG recovers part of the lost traffic (green points). As only three variables are represented, this interpretation is similar to that obtained for the ternary diagram (Fig. 3).

Fig. 4 Covariance Biplot. BALG-BAR-VAL traffic composition. The projection represents 100% of variance. The longitude of the rays is proportional to the variability of the clr.variable. Blue dots corresponds to the period 1976–1989 (before containerization boom), red dots correspond to the period 1990–2007 (before the crisis) and green dots correspond to the period 2008–2015

The cosinus of the angle between two links of the rays is an approximation to the linear correlation coefficient between the corresponding simple log-ratios. The links between the rays of clr(BALG)-clr(VAL) and clr(BALG)-clr(BAR)) are nearly orthogonal, suggesting a low correlation between these ratios. In fact, the correlation between $\ln(BALG/BAR)$ and $\ln(BALG/VAL)$ is -0.110. The correlation between $\ln(BAR/BALG)$ and $\ln(BAR/VAL)$ is 0.744, and finally $\ln(VAL/BALG)$ and $\ln(VAL/BAR)$ is 0.747. These values confirm the relative dependence of BAR with the others ports. In opposite, BALG has a more differentiated behaviour. In any case, the obtained values of correlation between the log-ratios is consistent with the previous analyses of the rays.

In order to deepen the interpretation of the evolution of the traffic composition, an ilr transform of the components has been also performed. The selected sequential binary partition (SBP) corresponds to Table 3. From the selected SBP, two balances are built:
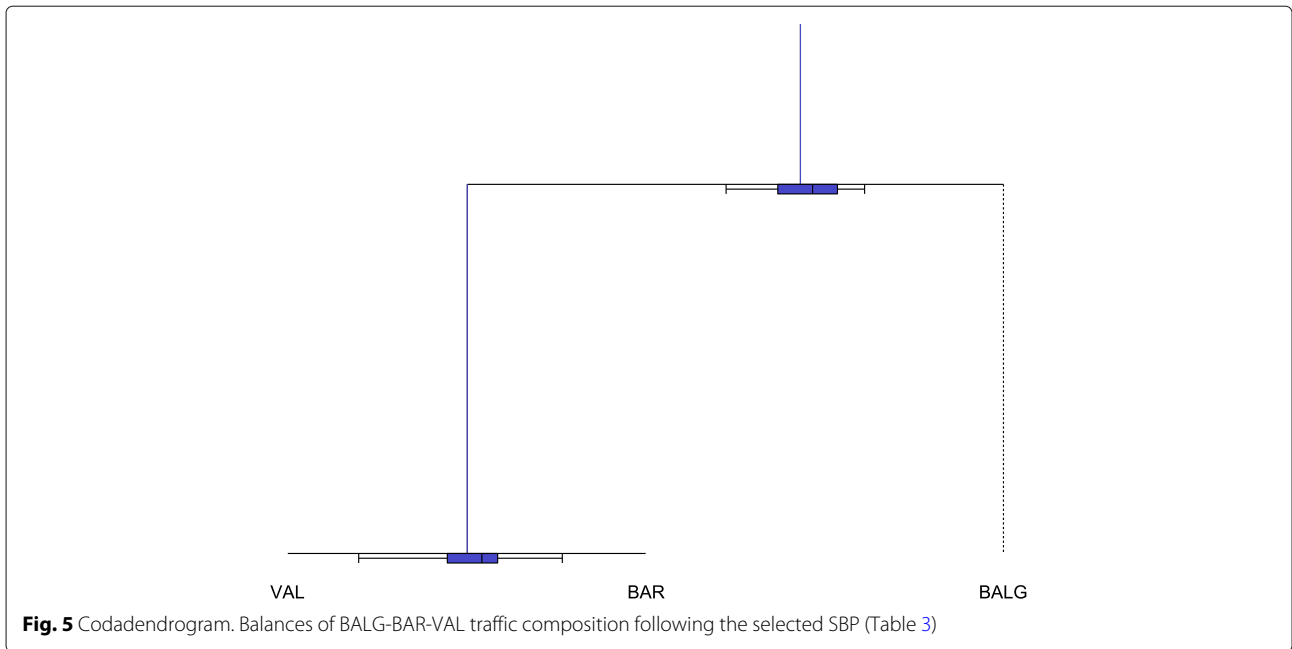
$$b_1 = \sqrt{\frac{2}{3}} \ln \left(\frac{BALG}{\sqrt{BAR \cdot VAL}} \right) \quad ; \quad b_2 = \sqrt{\frac{1}{2}} \left(\frac{BAR}{VAL} \right),$$

(11)

where the first balance accounts for the logratio between BALG port and the geometric mean of the other two ports, and the second balance is the logratio of BAR port versus VAL port.

The codadendrogram (Fig. 5) is an useful exploratory tool that helps with the description of these balances. This graphical representation also shows the ilr decomposition of the total variance, as well as the mean and dispersion of each balance. The length of the blue vertical bars shown in Fig. 5 is proportional to the variance of the balance [14, 27]. In this case, the second balance, BAR vs. VAL, has a higher variance than the first one (BALG vs the geometric mean of BAR and VAL). The point where these verticals bars join the horizontal bars is the mean balance, i.e. the coordinate corresponding to the sample center (Eq. 4). For both balances this point is close to the middle of the horizontal bar. This is consistent with the mean of the balances that are 0.243 and 0.003 for each balance. The figure also shows a characterization of the ilr dispersion through a box-plot of the corresponding balance, where balance ranges and quartiles are also presented (see example in [28]). In the figure, the box-plot of the first balance shows some asymmetry and more dispersion than the box-plot of the second balance.
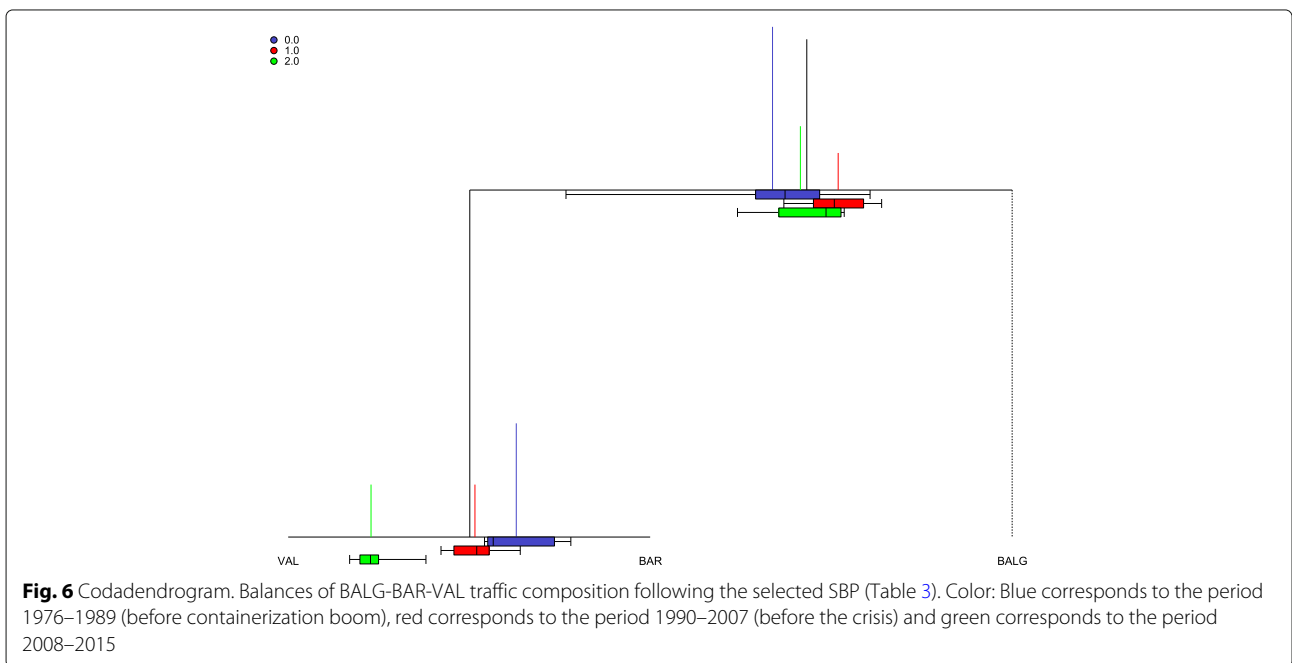
Table 3 Sequential Binary Partition for the three big ports

Balance	BALG	BAR	VAL
b_1	1	-1	-1
b_2	0	1	-1

Fig. 5 Codadendrogram. Balances of BALG-BAR-VAL traffic composition following the selected SBP (Table 3)

The addition of a factor variable to the codadendrogram may be also useful. Figure 6 shows the codadendrogram corresponding to the selected SBP, adding a time-evolution factor: the initial years (blue lines), the containerization boom period (red lines) and the post-crisis years (green lines). The figure shows some changes in the balances. The vertical bars corresponding to the initial years of the balances show a higher variance than the bars corresponding to the next years. This is due to the fluctuations of the traffic share evolution without any

clear leadership in comparison to the subsequent periods (see Figures 2 and 3). The boom of containerization was marked by a leadership of the BALG in its traffic share, which meant small fluctuations in the traffic share evolution. This is reflected by the low coordinate variances (red vertical bars) in Fig. 6. Afterwards, the variance of the balances of the post crisis years increased, due to the different adaptation of the ports after the 2008 crisis. In this sense, the three ports behave very differently: VAL increases significantly its traffic due to the role that played the settling

Fig. 6 Codadendrogram. Balances of BALG-BAR-VAL traffic composition following the selected SBP (Table 3). Color: Blue corresponds to the period 1976–1989 (before containerization boom), red corresponds to the period 1990–2007 (before the crisis) and green corresponds to the period 2008–2015
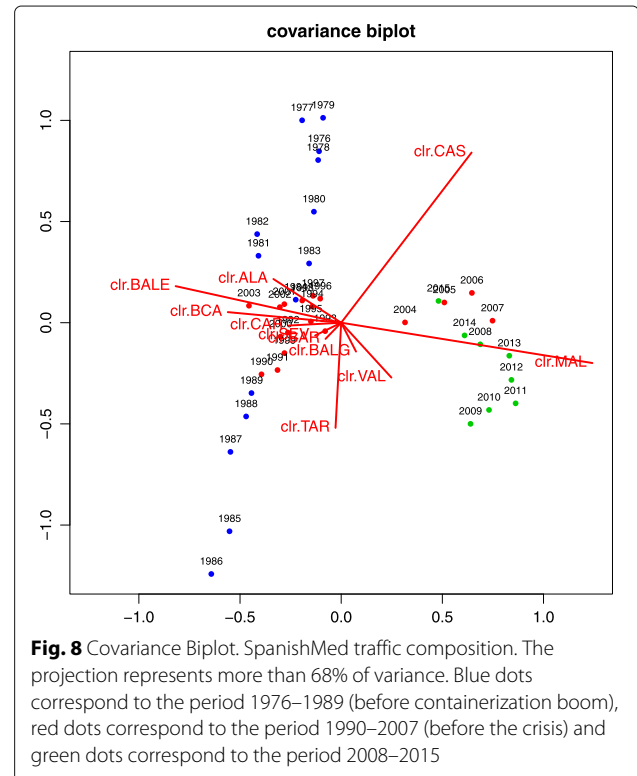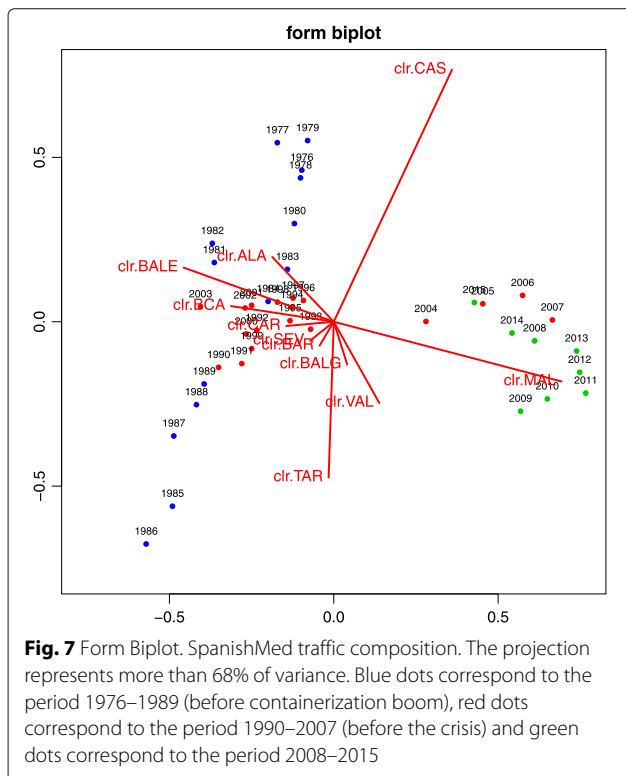
of MSC base in 2002, BALG maintains its relevance after post-crisis fluctuations in its traffic share and BAR loses its influence in the sub-composition. The center of the first balance changes only slightly for the three periods. In opposite, the changes are significant for the second balance (VAL vs BAR), showing an increasing influence of the VAL port.

5 SpanishMed container throughput: a compositional data (CoDa) approach

Once the sub-composition of the three main ports has been analysed using CoDa, all the SpanishMed ports are considered. Figure 2 shows the total container throughput and the correspondent traffic share evolution. Figure 2 (right) shows a zoom of the total traffic to highlight the temporal evolution of the smaller ports. Figure 7 shows the form clr-biplot for the container throughput composition of the SpanishMed ports. It corresponds to the projection on the two first components and accounts for 68% of the total variability. The three first components account for 86% of the variance. The low alignment pattern of the rays (spreading of the variables in the form clr-biplot) also indicates the relative low explanation of the new projection axis. The form clr-biplot helps with the assessment of which variables are better represented in the projection. Ideally, if all the variables were well represented in the projection, the rays would have the same length. In the Fig. 7, CAS(Castelló), MAL (Malaga) and BALE (Balearic Islands) ports are the ones with a better

representation on this projection. Also, these ports are the ones with more variability, following the covariance biplot (Fig. 8). These three ports (BALE, CAS and MAL) show large rays; this is due to its small container volume implying that their relative changes are larger meaning more volatility. For instance, MAL port had a large volatility in its traffic share being relevant during 2012 (4.7%) as opposed to years 1985, 2000 or 2015 (see Table 1). CAS is characterized by a gentle increase of the traffic share after 2000 being the fourth port in importance in total throughput and traffic share during 2015. This pattern is not followed by other ports and therefore CAS port appears isolated in the first quadrant of the projection. Also, a high volatility in the traffic share is observed in BALE, which shifted from 8.20 to 0.75% of the traffic from 1985 to 2015 (note that this evolution is clearly different to the MAL case, consistently with the interpretation of the clr-biplot). The other ports are not represented so well in this projection, probably due to their smaller variability.

Some ports (e.g. ALA (Alacant), BALE, BCA (Cádiz Bay)) show a nearby location in the projection on the covariance clr-biplot. This set of ports has a similar pattern of variability, in particular a gentle decreasing of traffic share from 1985 to 2015 (see Table 1). According to the covariance clr-biplot, also a similar pattern is observed for the set of ports formed by SEV (Sevilla), BAR and CAR (Cartagena). According to Table 1 this behavior is associated with a relative loss of traffic share in 2015 in comparison to 1985. The alignment of the rays of BALG,

Fig. 7 Form Biplot. SpanishMed traffic composition. The projection represents more than 68% of variance. Blue dots correspond to the period 1976–1989 (before containerization boom), red dots correspond to the period 1990–2007 (before the crisis) and green dots correspond to the period 2008–2015

Fig. 8 Covariance Biplot. SpanishMed traffic composition. The projection represents more than 68% of variance. Blue dots correspond to the period 1976–1989 (before containerization boom), red dots correspond to the period 1990–2007 (before the crisis) and green dots correspond to the period 2008–2015

BAR and VAL (the three big ports) also indicates that the three ports do no have a very different pattern in comparison to other ports. Figures 7 and 8 also shows the temporal evolution of the CAS port traffic share. During the eighties this port lost importance, recovered during the nineties. The evolution since 2004 is toward a composition where the MAL port gains importance, but the figure also shows the evolution of the parts of the three more important ports (BAR-BALG-VAL). These three ports are not very well represented in the projection, and are characterized by a small variability until 2012, when its importance started to decrease. These figures also show that since 2004 the SpanishMed traffic composition evolves from a BAR influence area to a VAL influence area, consistent with the findings in Section 4 and agreeing with the sub-compositional coherence principle [28].

The relationship between clr-variables may be also assessed through the covariance clr-biplot. In the figure, the links between the rays clr(BALE)-clr(CAS) and clr(CAS)-clr(MAL) are nearly orthogonal and therefore the corresponding simple log-ratios present low correlation. When computed, the corresponding linear correlation coefficient between ln(BALE/CAS) and ln(CAS/MAL) is -0.18. The orthogonality of links is clearer for the clr(BALE)-clr(MAL) and clr(VAL)-clr(CAS). The linear correlation coefficient corresponding to their log-ratios, ln(BALE/MAL) and ln(VAL/CAS) is 0.05. An additional assessment of the relationships between pairs of ports is provided by the variation matrix (Table 4). In this case, substantial log-ratio normalized variances agree with the clr-biplots interpretation (i.e. clr(BALE)-clr(CAS) equals to 3.033 and clr(MAL)-clr(CAS) equals to 2.827. The smallest contributions are the ones between the clr(BAR) and clr(BALG) variances (0.146), followed by the contributions which relate ports

such as ALA, SEV or VAL (see clr-variances in Table 4). This confirms the assessment provided by the covariance clr-biplot, where the rays corresponding to these ports are proportional (showing a similar pattern) and the contribution to variability is redundant. The largest contribution to variability is provided by MAL (clr-variances equals to 2.075) and CAS (clr-variances equals to 1.360) consistent again with the assessment of the clr-biplot: there is a low correlation of both variables with the other ports.

For further assessment of the SpanishMed traffic composition, an ilr transformation has also been performed. The selected SBP is shown in Table 5. The corresponding balances compare ports with different characteristics. For instance,

$$b_1 = \sqrt{\frac{10}{11}} \ln\left(\frac{BALE}{g(\text{rest})}\right) \quad ; \quad b_4 = \sqrt{\frac{1}{2}} \ln\left(\frac{BAR}{VAL}\right),$$

(12)

$$b_2 = \sqrt{\frac{21}{10}} \ln\left(\frac{(BALG \cdot BAR \cdot VAL)^{1/3}}{g(\text{remaining 7 ports})}\right).$$

Some of the criteria used to build the balances are described as follows. Balance b_1 corresponds to the balance of BALE port with the geometric mean of the rest of the ports. The insular nature of this port suggests a low dependence with the others and consequently a high variability of the balance. The second balance b_2 corresponds to the comparison of the geometric mean of the three big ports with the geometric mean of the non-insular ports of the system. Due to the subcompositional coherence of the compositional treatment of the shares, b_3 and b_4 coincide with Eq. 11, that is, the balances that compare the sub-system of the three big ports.

Table 4 Log-ratio normalized variances of the traffic throughput yearly compositions

	ALA	BALG	BCA	BALE	BAR	CAR	CAS	MAL	SEV	TAR	VAL	Clr-var
ALA	0.0	0.850	0.165	0.384	0.371	0.146	1.748	3.172	0.555	1.287	0.988	0.261
BALG	0.850	0.0	1.160	1.311	0.146	0.560	1.767	3.172	0.555	1.287	0.987	0.254
BCA	0.165	1.160	0.0	0.249	0.579	0.281	2.647	3.702	0.723	1.429	1.337	0.498
BALE	0.384	1.311	0.249	0.0	0.740	0.556	3.033	4.804	1.020	1.870	1.701	0.807
BAR	0.372	0.146	0.579	0.740	0.0	0.219	1.688	2.312	0.467	0.792	0.216	0.067
CAR	0.146	0.560	0.281	0.556	0.219	0.0	1.837	2.869	0.381	0.808	0.619	0.135
CAS	1.748	1.767	2.647	3.033	1.688	1.837	0.0	2.827	2.083	2.389	1.736	1.360
MAL	3.172	2.162	3.702	4.805	2.313	2.869	2.827	0.0	2.557	3.415	1.795	2.075
SEV	0.555	0.659	0.723	1.020	0.467	0.381	2.083	2.558	0.0	1.159	0.762	0.325
TAR	1.287	0.872	1.429	1.870	0.792	0.808	2.389	3.415	1.159	0.0	0.726	0.723
VAL	0.988	0.103	1.337	1.701	0.216	0.619	1.736	1.795	0.762	0.726	0.0	0.290
cen(x) (%)	3.10	34.1	2.9	4.6	25.4	1.0	0.7	0.4	1.5	0.9	25.3	

The bottom row contains the center of the sample and the right column contains the clr-variances

**Table 5** Sequential Binary Partition for the SpanishMed port system

Balance	ALA	BALG	BCA	BALE	BAR	CAR	CAS	MAL	SEV	TAR	VAL
b_1	-1	-1	-1	1	-1	-1	-1	-1	-1	-1	-1
b_2	-1	1	-1	0	1	-1	-1	-1	-1	-1	1
b_3	0	1	0	0	-1	0	0	0	0	0	-1
b_4	0	0	0	0	1	0	0	0	0	0	-1
b_5	-1	0	-1	0	0	-1	-1	1	-1	-1	0
b_6	-1	0	-1	0	0	-1	1	0	-1	-1	0
b_7	-1	0	-1	0	0	-1	0	0	-1	1	0
b_8	-1	0	-1	0	0	1	0	0	-1	0	0
b_9	1	0	-1	0	0	0	0	0	-1	0	0
b_{10}	0	0	1	0	0	0	0	0	-1	0	0

The codadendrogram of the SpanishMed ports balances, following the selected SBP (Table 5), is shown in Fig. 9. The vertical bars, proportional to the variances of the balances, show very different lengths. The longer bar corresponds to the fifth balance, that is the balance of the MAL port with respect to the geometric mean of the remaining ports. The second longer bar corresponds to the balance of CAS port with the geometric mean of the remaining ports (b_6). The fifth balance (Eq.12) also shows a mean balance that is clearly far from zero. This means that this balance (associated to MAL port) has relevant fluctuations during the analysed period. These interpretations are consistent with the conclusions drawn from Fig. 7 in regard to MAL and CAS ports. For other balances, for instance for the last balance (SEV vs BCA), the mean is likely zero. The box-plots show also different ilr variability patterns. For instance, the second balance shows a large ilr-dispersion, with some

asymmetry. This is related to the specific characteristics of the traffic share evolution of MAL port, previously explained. Other balances, for instance the VAL-BAR balance, show not only more ilr-symmetry, but also less ilr variability.

The introduction of the temporal evolution factor to the codadendrogram shows changes in the variances of the balances (Fig. 10). During the initial years, the variance of the market (blue vertical lines) is large in comparison to the subsequent periods. This is due to the small differences among the traffic share evolution in comparison to the boom of containerization when three ports rule the market. It means, the evolution in a concentrated market (see $H*$ in Table 1) implies larger variability. For some of the balances, the evolution of the mean balance is clearly observed. For instance, the balance CAS vs the geometric mean of the remaining ports shows an evolution of the mean balance towards CAS, i.e. the proportion of traffic share of CAS port respect the geometric mean of the remaining ports is higher after the crisis than in the early years (see Fig. 2). This is consistent with the interpretation of the clr-biplot (Fig. 8) and the traffic share evolution shown in Table 1.

As mentioned in Section 3, one of the principles of compositional analysis is subcompositional coherence. In our case, this condition means that the statistical results obtained through the analysis of the whole Spanish port system and the analysis of the subsample formed by BALG, BAR and VAL are coherent. In fact, the selected SBPs lead to the same results. For instance, the balance b_2 for the subcomposition (see Table 3) and the balance b_4 for the total SpansihMed analysis are the same. These balances correspond to the ratio BAR vs VAL. The analysis of the balance from both points of view (Figs. 6 and 10) shows a temporal evolution with a shift of the center of the balance towards VAL port.


Fig. 9 Codadendrogram. SpanishMed balances of traffic composition following the selected SBP (Table 5)
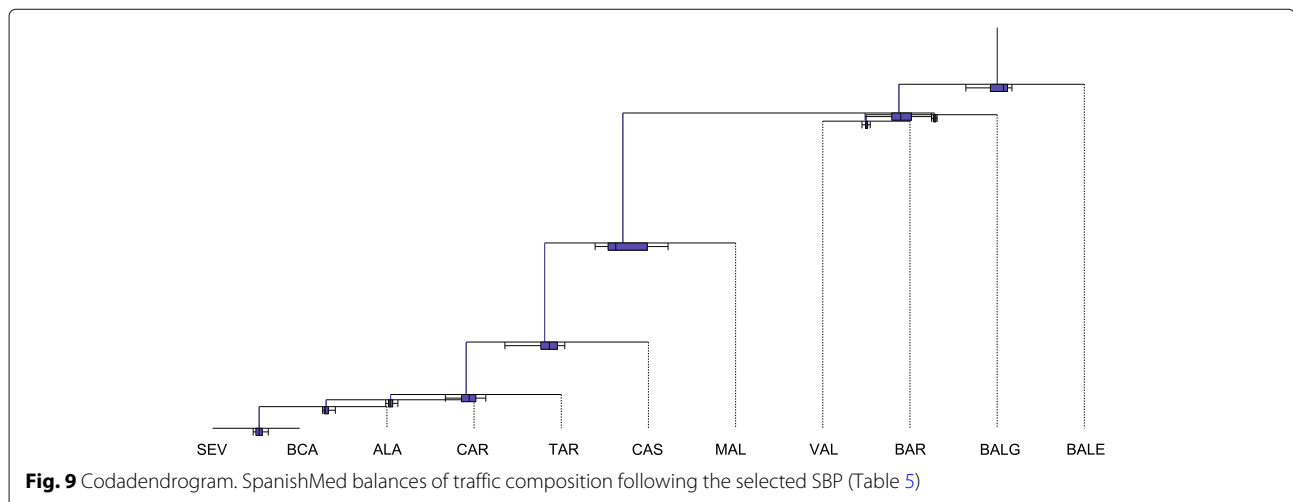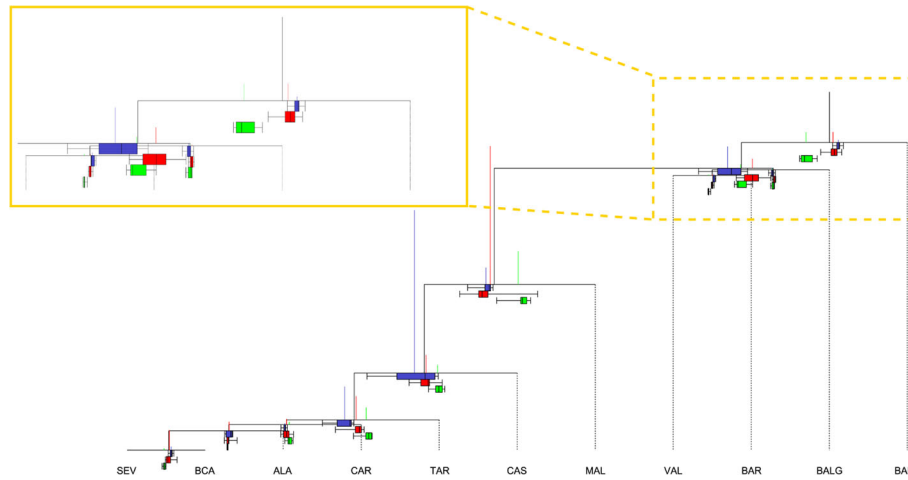
Fig. 10 Codadendrogram. SpanishMed balances of traffic composition following the selected SBP ((Table 5). Color: Blue corresponds to the period 1976–1989 (before containerization boom), red corresponds to the period 1990–2007 (before the crisis) and green corresponds to the period 2008–2015. The yellow box show a zoom of the BALG-BAR-VAL balances that is coherent with Fig. 6

The temporal evolution of the balances also suggests an interpretation of the temporal evolution of the traffic share among the ports. Figure 11 shows the balances time-series for the three big ports: b_1 and b_2. The balance b_1 shows a significant temporal variability without a clear trend during the analysed period. In opposite, the b_2 balance shows a negative slope which means that BAR port loses traffic share in front of VAL (see Eq.11). Figure 11 also shows the b_2 balance time-series (the three main ports vs the non-insular ports) when all the SpanishMed container system is investigated. The time-series shows how the big-ports gain importance in front of the small ports until 2002. Then a fluctuation period occurs before and after the crisis.

6 Discussion
In the framework of the ocean container transport and shipping, CoDa techniques help with the interpretation of the dependencies in the growths of traffic shares. The description of the evolution of the traffic share is not simple. Ocean container traffic is a complex and multi-faceted system where shippers, logistic services providers and shipping lines do not necessarily choose a port or port system, but they select a chain in which a port is merely a node [25]. From a historical point of view there is an increase of the traffic growth responding to the boom of the containerization jointly with the emergence of the global transport networks [18]. However, not all ports respond in the same way: the evolution of the SpanishMed
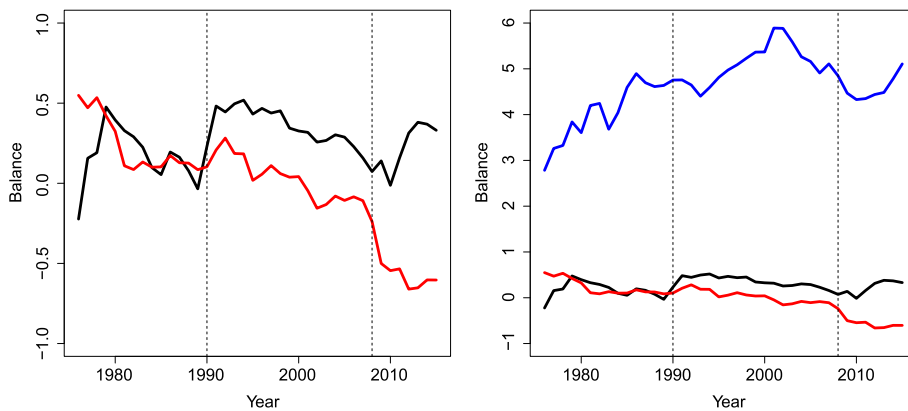
Fig. 11 (left) Evolution of the balances corresponding to the three big ports following the selected SBP (Eq. 11). First balance b_1 (black line); second balance b_2 (red line). (right) Evolution of three selected balances of the SpanishMed ports following the selected SBP (Table 5). The blue line shows the evolution of the balance that compares the three big ports with the rest of the non-insular ports (b_2; Eq. 10). Black and red lines represent the balances between the three big ports, according to the selected SBP (b_3 and b_4). Note that the compositional treatment of the shares ensures subcompositional coherence. Black and red lines are the same in left and right figures. Vertical lines show the limits of the three periods discussed

ports has evidenced a gradual increase in the concentration of activities in only a few ports (see Herfindahl-Hirschman index and Aitchison norm in Table 1). The need to implement economies of scales has led to two different port orientations in function of the market: large load centres or hubs (oriented to receive deep sea intercontinental ships) and smaller regional or feeder ports (with a prevalent percentage of import/export or feeder activity). Bahía de Algeciras (BALG) and Valencia (VAL) are examples of the former and Barcelona (BAR) an example of the latter. The inclusion of CoDa techniques has allowed to confirm this tendency from an analytic point of view. In particular, the data association and dependencies obtained by the clr-biplot evidences the connection between BAR and the other ports. Barcelona lost traffic share (due to a decrease of transshipment flows) in favor to the hubs of VAL and BALG as a result of the competition dynamics. This conclusion is not only obtained through the clr-biplot assessment, also the ternary plot interpretation and the computation of the linear correlation between the log-ratios agree to this point. This example illustrates the potentiality of CoDa methods in the traffic share description in a transport system being consistent with other authors (e.g. [24] or [9]).

The difference of magnitudes of the container throughput among different ports (for instance the container throughput in VAL port is 100 times larger than for Málaga (MAL) port) evidences the potentially of the CoDa methodology where the interest lies in the relative magnitude and variations within the system instead of the absolute values. It is worth mentioning the ability of CoDa analysis to investigate the patterns of evolution of small ports. Their behaviour may be hidden using conventional techniques. This is the case of CAS port, which traffic share evolution is uncorrelated with the other ports. CAS port has been able to capture and consolidate an alternative in the container throughput market in the SpanishMed system. In this sense, BALE and MAL ports also show a differentiated pattern. The rest of the ports reveal a similar pattern of variability in comparison to the mentioned ones. In consequence, relationships and similarity patterns have been detected. The loss of importance of the Barcelona (BAR) port has also been noted in the analysis of the results, where the turnover point of the total container throughput during 2008 has been pointed out. The global economic crisis during 2008 or the exceptional development of Valencia port in terms of container throughput have also been detected using CoDa descriptive tools. The assessment of the temporal evolution of the balances has allowed to investigate the response of the ports against the crisis among other interesting features. For instance, the balance b_3 time-series (Fig. 11) shows how the traffic share of the big ports is maximum during 2002 after a gentle increase. The subsequent decrease of

the contribution of the big ports may be associated with the "challenge of the periphery" [24] where new incomers appear with substantial traffic share (for instance CAS port) due to the congestion of existing big ports or the increase of the connectivity of the smallest ones. This tendency is also maintained during period 2008–2010, where it seems that the smallest ports experienced better resilience to the crisis. Finally, the three big ports recover importance during the period 2013–2015 probably due to the traffic retrieval in BAR port. Since the examined ports is a state-owned system, the investigation may have policy implications related to port categorization, competitive evaluation or resource assignment based on traffic share evolution.

The benefit of CoDa techniques to investigate transport disciplines is clear. Standard statistical techniques, based on the real Euclidean space, may provide misleading information about relations or similarity of the temporal evolution port traffic share. Temporal evolution of the market concentration/deconcentration is a typical approach to identify the variability of the traffic in a system. For instance, this analysis has been carried out on airports and air-flight companies (e.g. [30] or [26]) using concentration indexes (Herfindahl-Hirschman or Gini coefficients). This kind of analysis may reveal opportunities and threats for future investments in various types of transport infrastructure [30]. In SpanishMed, the inclusion of CoDa techniques has complemented the interpretation of H^* evolution and the Aitchison distance with its link with the variability of the market in the early years. Other areas of transportation engineering such as modal competiton or service complementarity may be benefited from using the CoDa approach. Other research works applying CoDa on socio-economic problems, such as [31] or [28], have revealed promising results identifying particular patterns on data as uneven as nutrition, social science or production engineering.

Two different CoDa transformations have been used, both following a log-ratio approach. The clr-transformation is useful in combination with statistical techniques based on distances, such as the biplot. The clr-biplot is a graphical representation that enhances the interpretability of the log-ratios. However, this transformation corresponds to a change of coordinates on a non-orthogonal basis, and the zero-sum of the obtained coordinates leads to a singular covariance matrix. As an alternative when these characteristics are a drawback, [13] introduced the isometric log-ratio transformation. The so-called balances are the coordinates of the composition in a real orthonormal basis. The basis may be selected using a sequential binary partition (SBP) which may enhance the interpretation. Future works may be related to the analysis of suitable Sequential Binary partitions and/or to expand the analysis of the obtained balances. For instance, the application of

ANOVA to the mean balances to assess if the differences are significant in the selected temporal periods. In the framework of port systems, the introduction of the CoDa techniques to the transshipment market may be useful. This market tends to be more unstable and volatile [25], so the inclusion of other kind of external variables [12] may be used in order to get insight into the market evolution.

7 Conclusions

The SpanishMed port system has been used as an example of introducing the CoDa methodology in transport disciplines. However, this is a wide applicable methodology, that should be applied to other geographical regions and other fields to understand the spatial integration that results in the movement of people and freight. The methodology has allowed to establish port associations, underlying patterns and to investigate tendencies avoiding spurious correlations that arise from the use of conventional statistical techniques. The original findings in the SpanishMed system analysis using CoDa is the emerging of small ports with a differentiated pattern (challenge of the periphery), the connection of the traffic share of Barcelona port with Valencia and Algeciras Bay ports (port competition) and the concentration process in the mentioned 3-big ports. The examined data and the practical conclusions may have relevant implications for policy makers due to the state ownership of the investigated port system.

Availability of data and materials
The datasets generated and/or analysed during the current study are available in the Spanish Port Agency (*Puertos del Estado*) repository: www.puertos.es.

Authors' contributions
MG conceived of the study and coordinate the CoDa statistical analyses and write the draft of the manuscript. MO participated in the design of the study and performed the CoDa statistical analysis. JJE read the draft version of the manuscript. All authors modified, read and approved the final manuscript.

Competing interests
The authors declare that they have no competing interests.

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